

5 The infinite set $S_2 = \{x: 0 < x < 1; x \in \mathbb{R}\}$ is bounded with supremum 1 and infimum zero, both of which do not belong to S_2 .

6 The infinite set $S_3 = \{x: 0 \leq x \leq 1; x \in \mathbb{R}\}$ is bounded with supremum 1 and infimum 0, both of which are members of S_3 .

7 The set $S_4 = \{\frac{1}{n}; n \in \mathbb{N}\}$ is bounded. The supremum 1 belongs to S_4 while infimum 0 does not.

(8) Each of the following intervals is bounded:

$$[a, b], (a, b], [a, b), (a, b).$$

Example (3): Prove that the greatest member of a set, if it exists, is the supremum (l.u.b) of the set.
(solution see after two pages)

Sol: let G be the greatest member of the set clearly $TS: - G \in \text{sup } S$.

(i) $x \leq G, \forall x \in S$.

so that G is an upper bound of S .

(ii) Again, no number less than G can be